Selected Topics in Ultrafast Optics

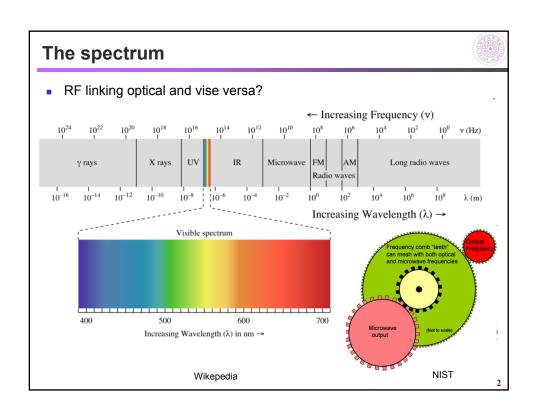
Generations and Applications of Optical Frequency Combs

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Motivations



- The definition of a second affects our daily living
 - Internet, GPS, cell phones....
- Other units related to a second
 - SI base units: meter, ampere, candela
 - SI derived units: volt (kg*m²/A*s³), Newton,....
- Physical constants
 - α decay rate, speed of light,.....
- High quality time and frequency standards an important task throughout the world

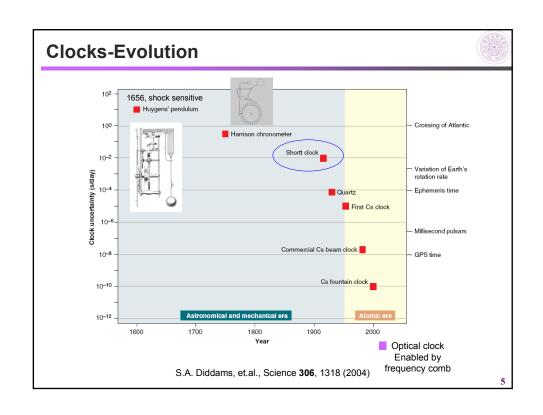
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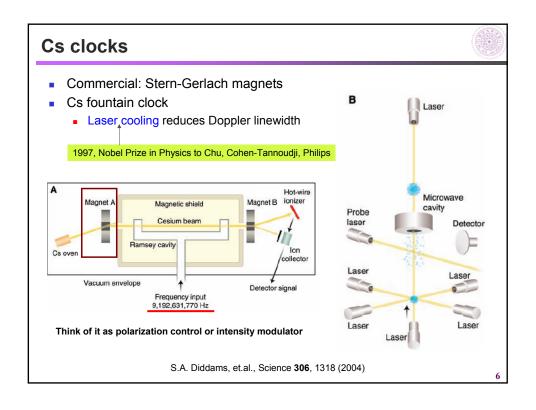
Definition of a second

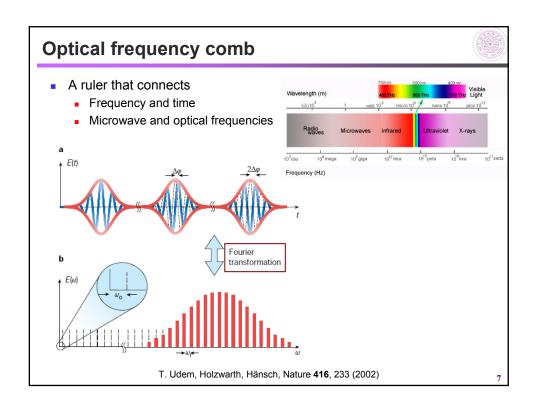


- 2000 B.C., Egyptians: divided day and night into 12 hours
- 1000, Muslims: counting the moon, (1/60)² of an hour
- 1670, Huygens pendulum
- 1956, the Ephemeris second: 1/31,556,925.9747 of Earth's one rotation around the Sun (a year) by the 11th General Conference on Weights and Measures
- 1967, the atomic time: 1/9,192,631,770 duration of ¹³³Cs ground-state transition by 13th General Conference on Weights and Measures
- 1980's, laser cooling made possible improved frequency stability in Cs clocks (Cs fountains)

$$\sigma_{y}(\tau) \approx \frac{\Delta v}{v_{0} SNR}$$



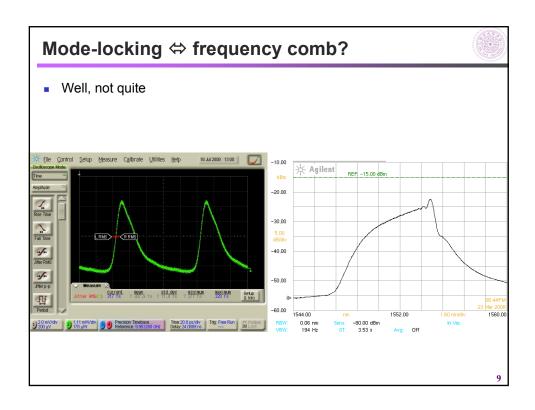




Bigger question



- So, if we have a pulse train, are we guaranteed a comb?
- Conversely, if we have a comb, are we guaranteed with a pulse train?



Realization of a "Comb"



- 1917, Einstein laid foundation for MASER and LASER
- 1953, Townes and students invented MASER
- 1957-60's, LASER theory developed by Townes and Schawlow
- 1960, first working laser (Ruby) by Maiman
- 1962, first semiconductor (GaAs) LD by R.N. Hall
- 1978, optical frequency comb envisioned

What took so long?

- 1998, frequency comb realized
- Explosion on this research field







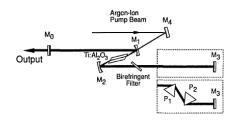


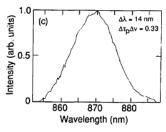
John L. Hall of NIST/JILA at Boulder, Colorado and Theodor W. Hänsch of Max-Plank Institute, Garching, Germany. (www.nobel.org)

What took so long?



- Laser introduced
 - Spectroscopy: CW laser
 - Nonlinearity: ultrafast community
- Late 1970's: spectroscopy using sub-picosecond
 - ~800 GHz "comb" that suffered huge frequency shift
- Kerr-lens mode-locking introduced in 1991
 - 60 fs pulses directly from Ti:S. But no one looked in frequency domain
- 1997, white light coherence of supercontinuum observed by Hänsch
- 1999, octave spanning spectrum with photonic crystal fiber
- 2004, intrinsic octave-spanning Ti:S





D.E. Spence, et.al.,, Opt. Lett. 16, 42 (1991)

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The milestone note



(CONFIDENTIAL)

Proposal for a universal optical frequency comb synthesizer

T. W. Hänsch Max-Planck-Institut für Quantenoptik

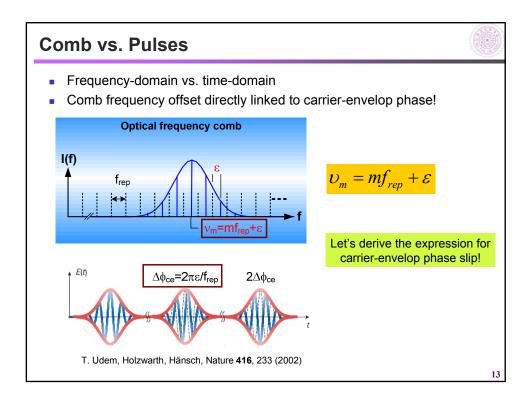
(March 30, 1997)

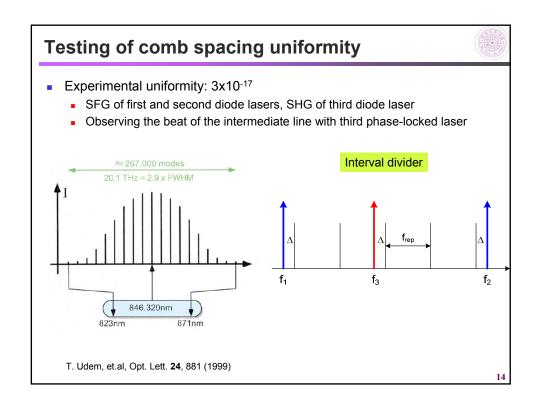
Abstract

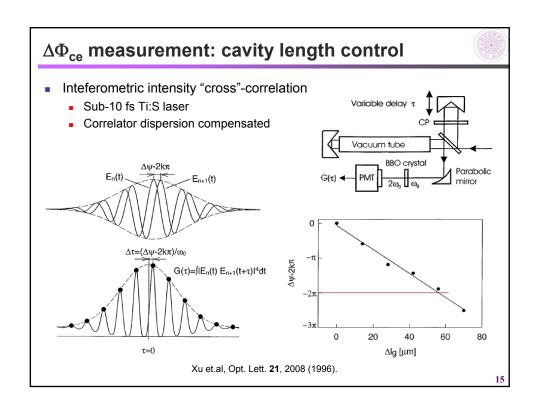
An optical frequency synthesizer is proposed which produces a wide comb of absolutely known equidistant marker frequencies throughout the infrared, visible, and ultraviolet spectral range. To this end, a white light continuum with pulse repetition rate f_p is produced by focusing the output of a mode-looked femtosecond laser into an optical fiber or bulk medium with a third order nonlinear susceptibility. The rate of phase slippage of the laser carrier relative to the pulse envelope f_a is monitored by observing a beat signal between the white light continuum and the second harmonic of the laser.

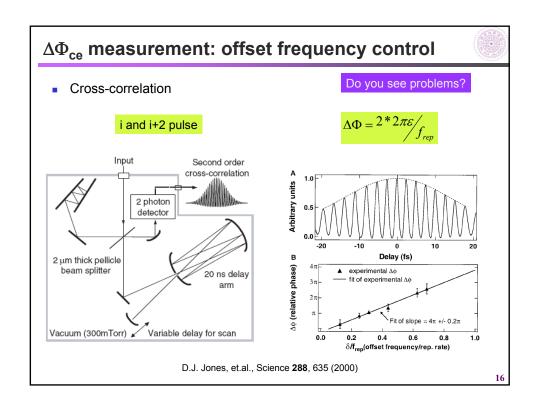
read and understood

http://nobelprize.org/nobel_prizes/physics/laureates/2005/hansch-lecture.html





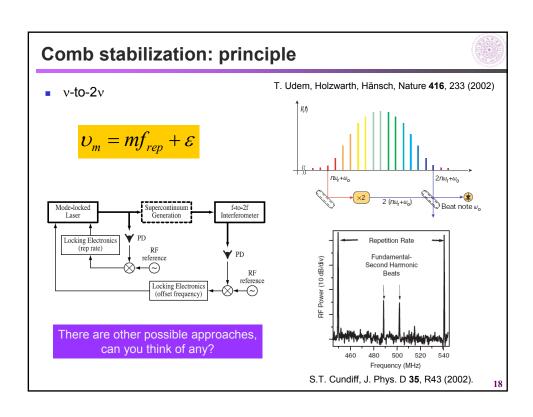


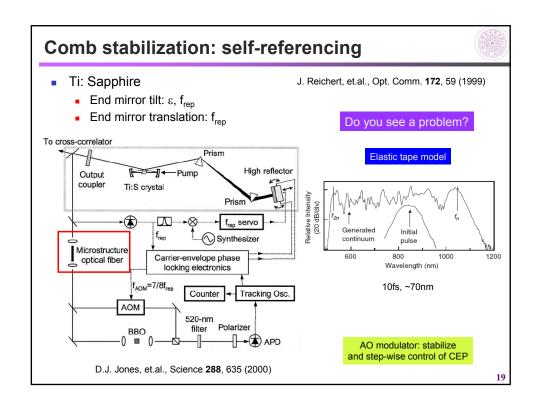


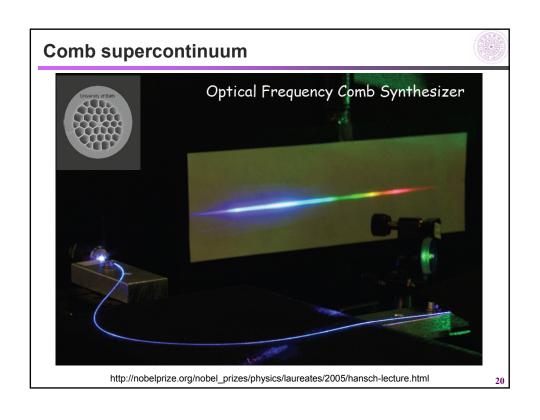
Absolute CEP measurement?

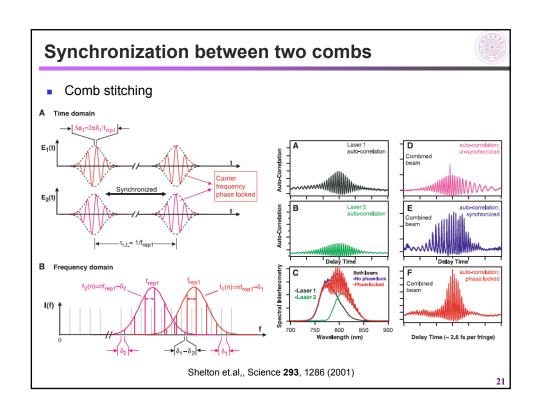


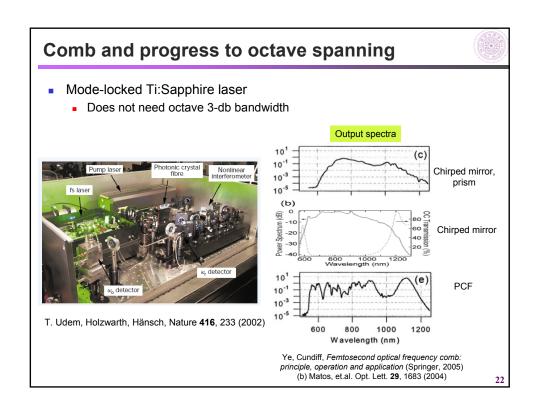
Anyone want to take this topic as your final report?







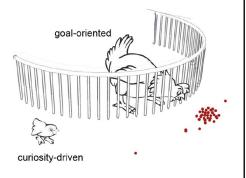




Comb applications



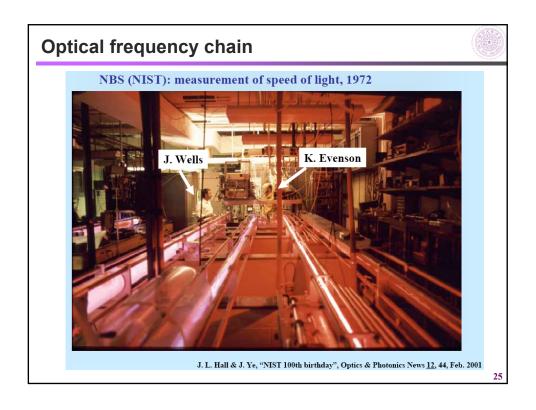
- Metrology: 1978...
- Optical clock
- Synthesis of ultra-purity optical and RF frequencies
- Remote transfer of time/frequency standards
- Precision spectroscopy
- Feel free to dream!

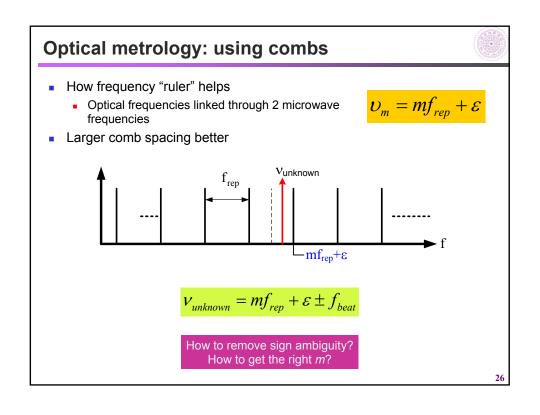


http://nobelprize.org/nobel_prizes/physics/laureates/2005/hansch-lecture.html

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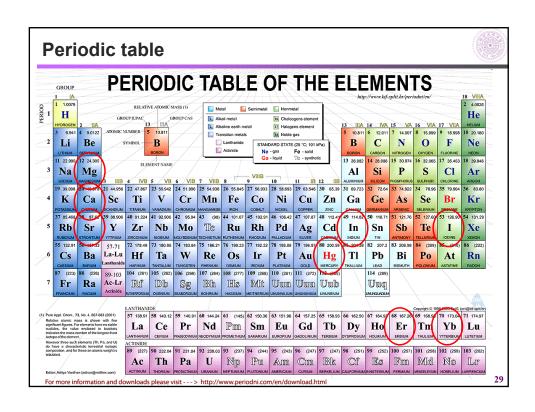
■ Multiplicative up-conversion ■ Complicated ■ Expensive ■ Not affordable unless \$\$\$ ■ Three labs, two buildings ■ Co₁-laser P(4) 2346464 Gifts PLL @ 10 Mile Co₂-laser P(4) 2346464 Gifts PLL @ 10 Mile PLL @ 10 Mile Co₃-laser P(20) 2347 105 Gifts PLL @ 10 Mile Co₄-laser P(20) 2347 105 Gifts Reputation 125 Gifts Co₄-laser P(20) 2347 105 Gifts Reputation 125 Gifts Repu





Fs comb measured frequencies				
• c	a 6 2H ₂ 1 r ⁺ 6 r ⁺ 2 b 7 5 b t a 6 g ⁺ 2 a 6	257 nm 257 nm 274 nm 243 nm 243 nm 243 nm 243 nm 257 nm 267 nm 267 nm 267 nm 267 nm 267 nm	Schnatz – PTB Nakagawa - NRLM Bernard – NRC v. Zanthier - MPQ Reichert - MPQ D. Jones - JILA Diddams - JILA Niering - MPQ Roberts - NPL v. Zanthier – MPQ Stenger – PTB Udem – NIST Udem – NIST Stenger – PTB	PRL 1 Jan '96 JOSA-B Dec '96 PRL 19 Apr '99 Opt.Comm. Aug'99 PRL 10 Apr '00 Science 28 Apr 00 PRL 29 May '00 PRL 12 June '00 PRA 7 July '00 Opt. Lett. 1 Dec. '00 PRA 17 Jan '01 PRL 28 May '01 Opt. Lett.15 Oct '01
	http://nobelprize.org/nobel_prizes/physics/laureates/2005/hall-lecture.html			

Optical clock 1950's: 133Cs at 9,192,631,770 Hz Allan deviation 2000: optical clock Narrow linewidth oscillator Narrow quantum transition Probe laser Frequency counter Much better instability: 105 better ideal Shorten measurement time Choices Detector & Laser Control Atom (Ca, Sr, Mg, H...) ■ Ion (Hg+, Yb+, In+, Sr+...) Molecule (I₂, CH₄, CO₂...) Frequency Counter Optical Cavity Ye, Cundiff, Femtosecond optical frequency comb: principle, operation and application (Springer, 2005)



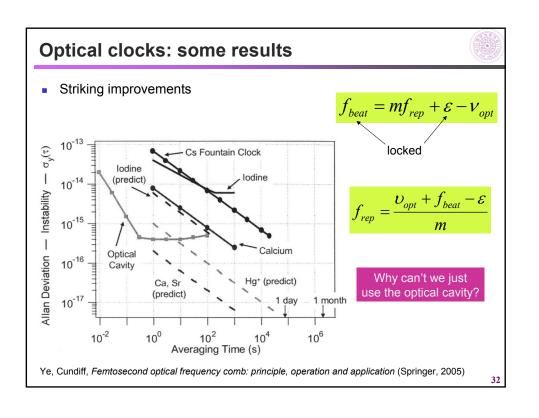
Molecular frequency standards ~1997

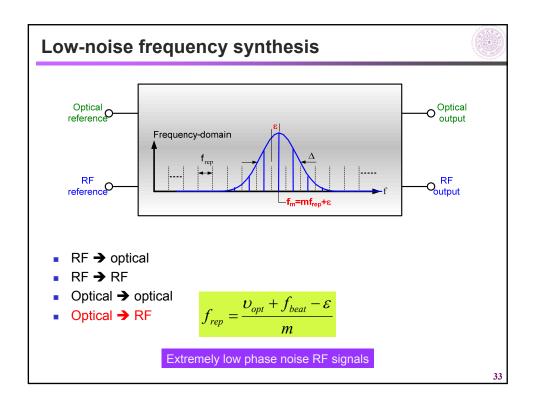


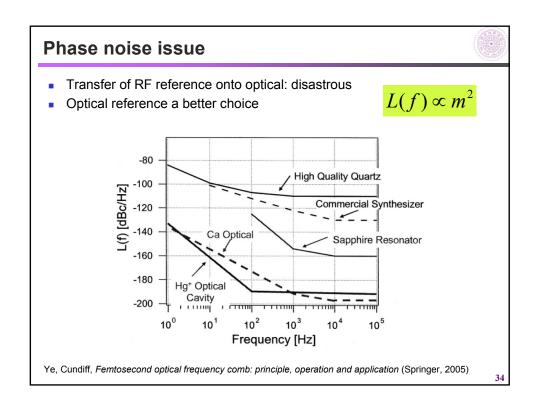
- HeNe Laser w CH₄ Absorber 3.39 μm
- HeNe vis Laser w I₂ Absorber ~5 vis λ's
- CO₂ Laser w CO₂ Absorber 10.6 μm
- CO₂ Laser w OsO₄ Absorber 10.6 μm
- Ar⁺ Laser w I₂ Absorber 514 nm
- Nd:YAG Laser w I₂ Absorber 1064 nm
- Nd:YAG Laser w C₂HD Abs. 1064 nm
- Yb:YAG Laser w C₂H₂ Abs. 1030 nm
- Diode Lasers w C₂H₂ Abs. 1550 nm

http://nobelprize.org/nobel_prizes/physics/laureates/2005/hall-lecture.html

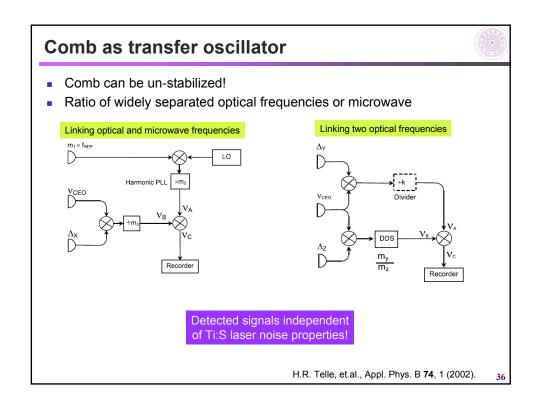
Hg⁺ optical clock Cooled ion that provides atomic transition (282 nm) Stabilized probe laser that provides the "clock tick" Optical frequency comb that provides an "optical" frequency divider Oscillator Oscillator Femitosecond laser Femitosecond laser Femitosecond laser Femitosecond laser Femitosecond laser S.A. Diddams, et.al., Science 306, 1318 (2004). 31







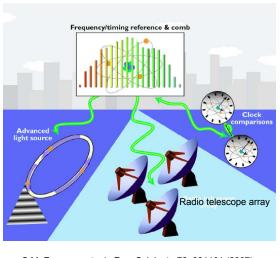
Removing ε dependence • Difference frequency generation • Sum frequency generation with an optical standard $f_b = v_{opt} + (n_{low}f_{rep} + \varepsilon) - (n_{high}f_{rep} + \varepsilon)$ $f_{rep} = \frac{v_{opt} - f_b}{n_{high} - n_{low}}$



Remote transfer



• Fiber as coherence transfer media



S.M. Foreman, et. al., Rev. Sci. Instr. 78, 021101 (2007).

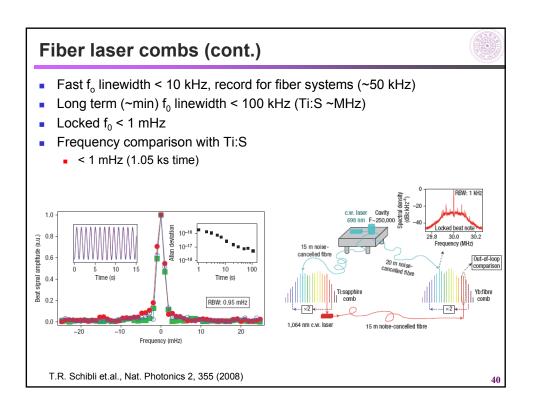
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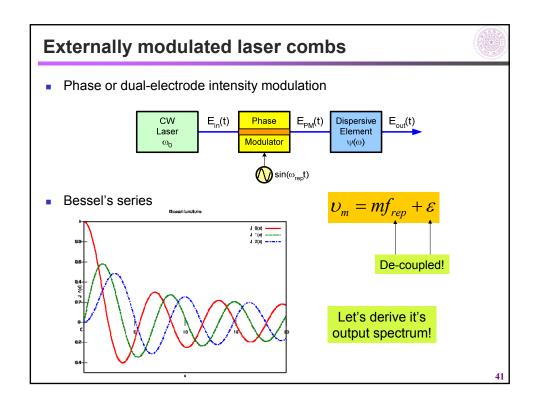
Comb alternatives

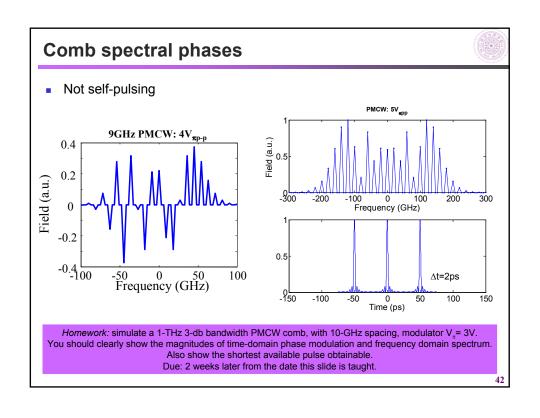


- Fiber laser combs
- Externally-modulated CW comb
 - Simple phase modulator
 - Dual-electrode intensity modulator
- Optical frequency comb generator
 - Actually dominated large-span optical frequency measurement during 1993-1998
- Compact comb generator using micro-toroid

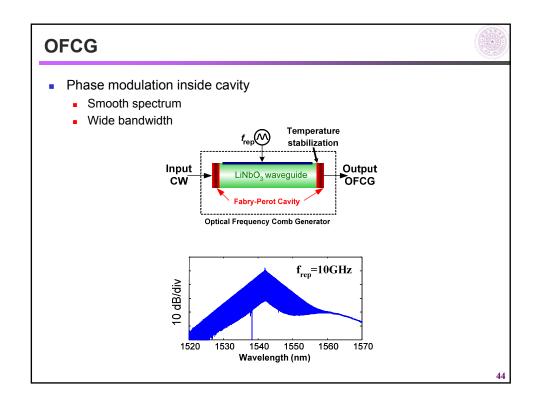
Fiber laser combs Compact, high power (>10 W) Different wavelength windows Cladding pumped CPA linear Er (1.5μm), Yb (1.05μm) amplification avoids nonlinearity induced phase and amplitude noise Best phase stability ever reported Single-mode fibre PM LMA Yb stretcher fibre power amplifier Yb doped SM fibre 915 nm Out-of-loop comparison -30 To other 1.200 698 nm 1,064 nm 698 nm: LD locked to Sr lattice optical clock T.R. Schibli et.al., Nat. Photonics 2, 355 (2008)

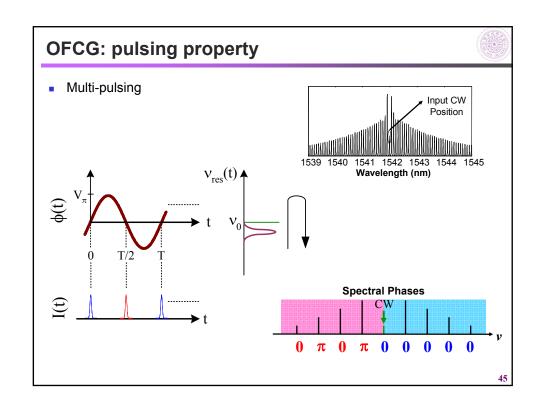


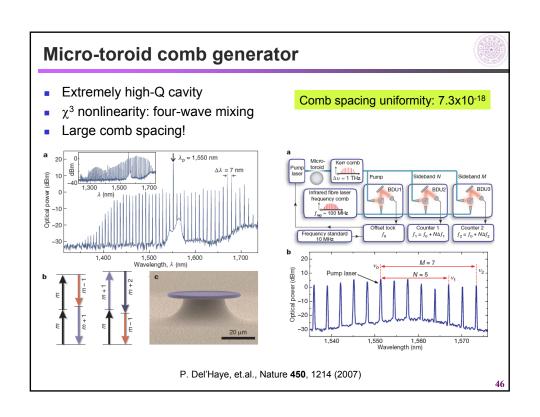




Flat externally modulated CW laser comb Dual electrode intensity modulator $\frac{P_k}{P_{in}} = \frac{1}{2\pi A} \{1 + \cos(2\Delta\theta)\cos(2\Delta A) + \frac{1}{2\pi A} \{1 + \cos(2\Delta\theta)\cos(2\Delta A)$







Summary



- History of a second and optical frequency comb explained
- Derivation and method for measuring the carrier-envelop phase slippage discussed
- Stabilization of OFC
- Applications of OFC
- Alternative OFC generations