# NATIONAL TSING HUA UNIVERSITY DEPARTMENT OF POWER MECHANICAL ENGINEERING 2011 Fall Semester

Course No.:	PME 510200
<b>Course Title:</b>	Multiscale Transport (多尺度傳輸)
	(Fluid, Molecule and Electron Flows)
Hours/Week:	T3 T4 R4
Classroom:	エー館 R 209
Teacher:	Prof. Che-Wun Hong (洪哲文教授)

**Objective:** This course covers the classical physics and modern physics developed from 19th to 21st centuries. The contents introduce the multiscale transport phenomena of fluid particles (continuum), molecules (non-continuum), electrons and photons (particle-wave duality). Mathematical models of each scale of flow models are derived and their exact solutions as well as numerical solutions will be explained. This is a general course for senior undergraduates, postgraduates from every background, including thermofluids, solid mechanics, optoelctronics, MEMS/NEMS groups.

#### **Contents:**

#### (1) Introduction to Multi-scale Transport

- 1.1 Development of Multi-scale Transport in Physics
- 1.2 Classical Physics and Modern Physics
- 1.3 Macroscopic and Microscopic Models
- 1.4 Micro Flow Examples
- 1.5 Macro Flow Development
- 1.6 Kinetic and Transport Properties of Fluids
- 1.7 General Boundary Conditions

#### (2) Macro Flow Models (The Navier-Stokes Equation)

- 2.1 Fundamental Equations
- 2.2 Conservation of Mass (Continuity Equations)
- 2.3 Conservation of Momentum (Navier-Stoke Equations)
- 2.4 Conservation of Energy (1st Law of Thermodynamics)
- 2.5 Summary of the Basic Equations
- 2.6 Examples of Boundary Conditions
- 2.7 Orthogonal Coordinate System
- 2.8 Mathematical Characters of the Basic Equations

- 2.9 Dimensional Analysis and Dynamic Similarity
- 2.10 Summary of the Basic Equations in CFD
- 2.11 Control Volume Formulations
- 2.12 Integral Form of the Generic Conservation Equation

#### (3) Analytical Solutions of the Continuum Flow

- 3.1 Classification of Solutions
- 3.2 Couette Flows
- 3.3 Poiseuille Flow through Ducts
- 3.4 The Circular Pipe: Hagen-Poiseuille Flow
- 3.5 Combined Couette-Poiseuille Flow between Plates
- 3.6 Noncircular Ducts
- 3.7 Temperature Distribution in Fully Developed Duct Flow
- 3.8 Thermal Entrance: The Graetz Problem
- 3.9 Creeping Flow (Low Reynolds Number Flow)
- 3.10 Lubrication Theory

## (4) Numerical Solutions of the N-S Equations (CFD)

- 4.1 Differential Form of the N-S Equations
- 4.2 Integral Form of the N-S Equations
- 4.3 Mathematical Characters of the Basic Equations
- 4.4 Finite Difference Methods for Elliptic Problems
- 4.5 Finite Difference Methods for Parabolic Problems
- 4.6 Finite Difference Methods for Hyperbolic Problems
- 4.7 Finite Difference Methods for CFD
- 4.8 Finite Volume Methods for CFD
- 4.9 Finite Element Methods for CFD

## (5) Micro Flow Models (The Boltzmann Equation)

- 5.1 Basic Equations for Micro Flows
- 5.2 Rarefied Gas Flows
- 5.3 Basic Kinetic Theory
- 5.4 The Boltzmann Equation
- 5.5 The Moment of the Boltzmann Equation
- 5.6 Conservation Equations
- 5.7 Exact Solution to the Boltzmann Equation
- 5.8 Micro Flows and Macro Flows

## (6) Numerical Solutions of the Lattice Boltzmann Model (LBM)

- 6.1 From the Boltzmann Equation to the Lattice Boltzmann Equation
- 6.2 BGK Lattice Boltzmann Model in 3D and 2D
- 6.3 Entropy and Equilibrium Distribution

- 6.4 Flow Chart of the BGK LBM Algorithm
- 6.5 Boundary Conditions
- 6.6 More Boundary Conditions

#### (7) Nano Flows (Molecular Dynamics)

- 7.1 Macro, Micro, and Nano Scales
- 7.2 Intermolecular Potential Models
- 7.3 Periodical Boundary Condition
- 7.4 Initialization
- 7.5 Equilibration
- 7.6 Fluid and Solid Mechanics
- 7.7 Radial Distribution Function
- 7.8 General Monte Carlo Methods

# (8) Introduction to Quantum Mechanics (The Schrödinger Equation)

- 8.1 Development of Quantum Mechanics
- 8.2 The Born Interpretation
- 8.3 Classical Wave Equations
- 8.4 The 1-D Simple Harmonic Oscillator
- 8.5 Wavefunction for a Free Particle
- 8.6 Wavefunctions in the Presence of Potential Forces
- 8.7 Numerical Method for the Schrödinger Equation
- 8.8 The Particle in a Box
- 8.9 The Finite Square Well
- 8.10 The Square Potential Barrier
- 8.11 Electron, Photon and Particle Statistics

## 8.12 Quantum Fluid Dynamics and Quantum LBM

## (9) Computational Quantum Mechanics (CQM)

- 9.1 Introduction
- 9.2 3-D Schrödinger Equation
- 9.3 Exact Solutions and Molecular Orbitals
- 9.4 The Periodic Table
- 9.5 General Poly-electronic Systems
- 9.6 The Energy of a General Poly-electronic System
- 9.7 The Hartree-Fock and Roothaan-Hall Equations
- 9.8 Ab Initio Method
- 9.9 Semi-empirical Methods
- 9.10 Density Functional Theory (DFT)
- 9.11 Multiscale Transport Examples

Lecture Notes: Supplement notes provided by PDF before each lecture

**References:** (1) "Viscous Fluid Flow"

F.M. White, 3<sup>rd</sup> Ed., McGraw-Hill, 2006

- (2) "Molecular Gas Dynamics and the Direct Simulation of Gas Flows", G.A. Bird, Clarendon Press, 1994.
- (3) "Lattice-Gas Cellular Automata and Lattice Boltzmann Models- An Introduction", D. A. Wolf-Gladrow, Springer, 2005
- "Modern Physics", 3<sup>rd</sup> Ed., R.A. Serway, C.J. Moses, C.A. Moyer, Thomson, 2005
- (5) "Simulating the Physical World: Hierarchical Modeling from Quantum Mechanics to Fluid Dynamics", 4<sup>th</sup> Ed., H.J.C. Berendsen, Cambridge Univ. Press, 2007
- Grades: Exercises (20%), Midterm Exam (40%), close book Final Exam (40%), open book