Linear Algebra, EE 10810/EECS 205004 Quiz 1.6

 $Integrity: {\rm There \ is \ NO \ space \ to \ cross \ the \ Red \ Line \ !!}$

1. Prove that

 $\text{if} \quad \{\overline{\overline{A}}_1,\overline{\overline{A}}_2,\ldots,\overline{\overline{A}}_k\} \quad \text{is a linearly independent subset},$

of $\overline{\overline{M}}_{n \times n}(F)$,

 $\text{then} \quad \{(\overline{\overline{A}}_1)^t, (\overline{\overline{A}}_2)^t, \dots, (\overline{\overline{A}}_k)^t\} \quad \text{is also linearly independent}.$

2. Do the polynomials $(x^3 - 2x^2 + 1)$, $(4x^2 - x + 3)$, and (3x - 2) generate $P_3(\mathcal{R})$?

3. Use the Lagrange interpolation formula to construct the polynomial of smallest degree whose graph contains the following points:

(-2, -6), (-1, 5), (1, 3).