

> # Set the parameters and functions

c := 'c':

d := 'd':

u := 'u':

E4 := (4572 c - 19890) u⁷ + (60582 c² + 36675 - 7620 d³ - 153630 d) u⁶ + (6096 c⁵ + 205290 c³ + 220050 c - 44808 d⁴ - 415215 d²) u⁵ + (11354 c⁶ + 300540 c⁴ + 550125 c² - 508 d⁷ - 97692 d⁵ - 518850 d³) u⁴ + (6858 c⁷ + 233370 c⁵ + 733500 c³ - 75915 d⁶ - 301950 d⁴) u³ + (75252 c⁶ + 550125 c⁴ - 21336 d⁷ - 93690 d⁵) u² + (220050 c⁵ - 6858 d⁷ - 63405 d⁶) u + 36675 c⁶ - 34290 d⁷:

print(Output);

find Sturm's sequence` `

for j from 0 by 1 to 179 do

c := $\frac{404}{100} + \frac{j+1}{180} \cdot \left(\frac{405}{100} - \frac{404}{100} \right)$:

d := $\frac{404}{100} + \frac{j}{180} \cdot \left(\frac{405}{100} - \frac{404}{100} \right)$:

u := 'u':

S := sturmseq(E4, u);

signnum := sturm(S, u, 4, $\frac{57}{10}$);

with(ArrayTools):

Slength := Size(S, 2);

X := Array(1..Slength);

Y := Array(1..Slength);

for i from 1 to Slength do

Find sgn $\left[s_{E_{4,i}}(0) \right]$

u := 4;

X[i] := signum(S[i]);

Find sgn $\left[s_{E_{4,i}}\left(\frac{57}{10}\right) \right]$

u := $\frac{57}{10}$:

Y[i] := signum(S[i]);

end do;

show the final results

print(['a'[j], 'a'[j+1], sgn(s['E'[4,j])(4)), sgn(s['E'[4,j])(5.7))] = [evalf(d, 5), evalf(c, 5), X, Y]);

end do:

Output

$[a_0, a_1, \text{sgn}(s_{E_{4,0}}(4)), \text{sgn}(s_{E_{4,0}}(5.7))] = [4.0400, 4.0401, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]]$

$[a_1, a_2, \text{sgn}(s_{E_{4,1}}(4)), \text{sgn}(s_{E_{4,1}}(5.7))] = [4.0401, 4.0401, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]]$

$[a_2, a_3, \text{sgn}(s_{E_{4,2}}(4)), \text{sgn}(s_{E_{4,2}}(5.7))] = [4.0401, 4.0402, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]]$

$[a_3, a_4, \text{sgn}(s_{E_{4,3}}(4)), \text{sgn}(s_{E_{4,3}}(5.7))] = [4.0402, 4.0402, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]]$

$$\begin{aligned}
& [a_{164}, a_{165}, \operatorname{sgn}(s_{E_{4,164}}^{(4)}), \operatorname{sgn}(s_{E_{4,164}}^{(5.7)})] = [4.0491, 4.0492, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]] \\
& [a_{165}, a_{166}, \operatorname{sgn}(s_{E_{4,165}}^{(4)}), \operatorname{sgn}(s_{E_{4,165}}^{(5.7)})] = [4.0492, 4.0492, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]] \\
& [a_{166}, a_{167}, \operatorname{sgn}(s_{E_{4,166}}^{(4)}), \operatorname{sgn}(s_{E_{4,166}}^{(5.7)})] = [4.0492, 4.0493, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]] \\
& [a_{167}, a_{168}, \operatorname{sgn}(s_{E_{4,167}}^{(4)}), \operatorname{sgn}(s_{E_{4,167}}^{(5.7)})] = [4.0493, 4.0493, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]] \\
& [a_{168}, a_{169}, \operatorname{sgn}(s_{E_{4,168}}^{(4)}), \operatorname{sgn}(s_{E_{4,168}}^{(5.7)})] = [4.0493, 4.0494, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]] \\
& [a_{169}, a_{170}, \operatorname{sgn}(s_{E_{4,169}}^{(4)}), \operatorname{sgn}(s_{E_{4,169}}^{(5.7)})] = [4.0494, 4.0494, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]] \\
& [a_{170}, a_{171}, \operatorname{sgn}(s_{E_{4,170}}^{(4)}), \operatorname{sgn}(s_{E_{4,170}}^{(5.7)})] = [4.0494, 4.0495, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]] \\
& [a_{171}, a_{172}, \operatorname{sgn}(s_{E_{4,171}}^{(4)}), \operatorname{sgn}(s_{E_{4,171}}^{(5.7)})] = [4.0495, 4.0496, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]] \\
& [a_{172}, a_{173}, \operatorname{sgn}(s_{E_{4,172}}^{(4)}), \operatorname{sgn}(s_{E_{4,172}}^{(5.7)})] = [4.0496, 4.0496, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]] \\
& [a_{173}, a_{174}, \operatorname{sgn}(s_{E_{4,173}}^{(4)}), \operatorname{sgn}(s_{E_{4,173}}^{(5.7)})] = [4.0496, 4.0497, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]] \\
& [a_{174}, a_{175}, \operatorname{sgn}(s_{E_{4,174}}^{(4)}), \operatorname{sgn}(s_{E_{4,174}}^{(5.7)})] = [4.0497, 4.0497, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]] \\
& [a_{175}, a_{176}, \operatorname{sgn}(s_{E_{4,175}}^{(4)}), \operatorname{sgn}(s_{E_{4,175}}^{(5.7)})] = [4.0497, 4.0498, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]] \\
& [a_{176}, a_{177}, \operatorname{sgn}(s_{E_{4,176}}^{(4)}), \operatorname{sgn}(s_{E_{4,176}}^{(5.7)})] = [4.0498, 4.0498, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]] \\
& [a_{177}, a_{178}, \operatorname{sgn}(s_{E_{4,177}}^{(4)}), \operatorname{sgn}(s_{E_{4,177}}^{(5.7)})] = [4.0498, 4.0499, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]] \\
& [a_{178}, a_{179}, \operatorname{sgn}(s_{E_{4,178}}^{(4)}), \operatorname{sgn}(s_{E_{4,178}}^{(5.7)})] = [4.0499, 4.0499, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]] \\
& [a_{179}, a_{180}, \operatorname{sgn}(s_{E_{4,179}}^{(4)}), \operatorname{sgn}(s_{E_{4,179}}^{(5.7)})] = [4.0499, 4.0500, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]]
\end{aligned}$$

(1)

