

> # Set the parameters and functions

c := 'c':

d := 'd':

u := 'u':

$$E4 := (4572 c - 19890) u^7 + (60582 c^2 + 36675 - 7620 d^3 - 153630 d) u^6 + (6096 c^5 + 205290 c^3 + 220050 c - 44808 d^4 - 415215 d^2) u^5 + (11354 c^6 + 300540 c^4 + 550125 c^2 - 508 d^7 - 97692 d^5 - 518850 d^3) u^4 + (6858 c^7 + 233370 c^5 + 733500 c^3 - 75915 d^6 - 301950 d^4) u^3 + (75252 c^6 + 550125 c^4 - 21336 d^7 - 93690 d^5) u^2 + (220050 c^5 - 6858 d^7 - 63405 d^6) u + 36675 c^6 - 34290 d^7 :$$

print(Output);

# find Sturm's sequence` `

for j from 0 by 1 to 199 do

$$c := \frac{405}{100} + \frac{j+1}{200} \cdot \left( \frac{408}{100} - \frac{405}{100} \right) :$$

$$d := \frac{405}{100} + \frac{j}{200} \cdot \left( \frac{408}{100} - \frac{405}{100} \right) :$$

u := 'u':

S := sturmseq(E4, u);

signnum := sturm(S, u, 4,  $\frac{57}{10}$ );

with(ArrayTools) :

Length := Size(S, 2);

X := Array(1 .. Length);

Y := Array(1 .. Length);

for i from 1 to Length do

# Find sgn  $\left[ s_{E_{4,i}}(0) \right]$

u := 4;

X[i] := signum(S[i]);

# Find sgn  $\left[ s_{E_{4,i}}\left(\frac{57}{10}\right) \right]$

u :=  $\frac{57}{10}$  :

Y[i] := signum(S[i]);

end do;

# show the final results

print([ 'a'[180 + j], 'a'[181 + j], sgn(s[ 'E'[4, 180 + j]](4)), sgn(s[ 'E'[4, 180 + j]](5.7)) ]  
= [ evalf(d, 5), evalf(c, 5), X, Y] );

end do:

### Output

$$\begin{aligned} & [a_{180}, a_{181}, \text{sgn}(s_{E_{4,180}}(4)), \text{sgn}(s_{E_{4,180}}(5.7))] = [4.0500, 4.0502, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]] \\ & [a_{181}, a_{182}, \text{sgn}(s_{E_{4,181}}(4)), \text{sgn}(s_{E_{4,181}}(5.7))] = [4.0502, 4.0503, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]] \\ & [a_{182}, a_{183}, \text{sgn}(s_{E_{4,182}}(4)), \text{sgn}(s_{E_{4,182}}(5.7))] = [4.0503, 4.0504, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]] \\ & [a_{183}, a_{184}, \text{sgn}(s_{E_{4,183}}(4)), \text{sgn}(s_{E_{4,183}}(5.7))] = [4.0504, 4.0506, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]] \\ & [a_{184}, a_{185}, \text{sgn}(s_{E_{4,184}}(4)), \text{sgn}(s_{E_{4,184}}(5.7))] = [4.0506, 4.0508, [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]] \end{aligned}$$













$$\begin{aligned}
& [a_{377}, a_{378}, \operatorname{sgn}(s_{E_{4,377}}^{(4)}), \operatorname{sgn}(s_{E_{4,377}}^{(5.7)})] = [4.0796, 4.0797, [-1 \ -1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]] \\
& [a_{378}, a_{379}, \operatorname{sgn}(s_{E_{4,378}}^{(4)}), \operatorname{sgn}(s_{E_{4,378}}^{(5.7)})] = [4.0797, 4.0798, [-1 \ -1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]] \\
& [a_{379}, a_{380}, \operatorname{sgn}(s_{E_{4,379}}^{(4)}), \operatorname{sgn}(s_{E_{4,379}}^{(5.7)})] = [4.0798, 4.0800, [-1 \ -1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1], [-1 \ 1 \ 1 \ 1 \ -1 \ -1 \ 1 \ -1]]
\end{aligned}$$

**(1)**